200 Exam Questions & Answers

- Show that (x + 2) is a factor of $f(x) = x^3 2x^2 4x + 8$ and hence fully factorise f(x).
- 162

Calculate the discriminant of the quadratic equation $2x^2 + 4x + 5 = 0$

163

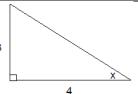
Solve the equation $log_4(5-x) - log_4(3-x) = 2$, x < 3.

164

Find all the values of x in the interval $0 \le x \le 2\pi$ for which $tan^2(x) = 3$.

165

Show that the exact value of cos2x is $\frac{7}{25}$.



166

If $y = 3\cos^4 x$, find $\frac{dy}{dx}$.

A curve has equation $y = x^3 - 3x^2 - 9x + 12$. Find the coordinates of the stationary points of this curve and determine their nature.

168

Find $\int \frac{4x^3-1}{x^2} dx$, $x \neq 0$.

169

Find the value of $\int_0^2 \sin(4x+1) dx$.

170

A curve has equation y=7sinx-24cosx. Express 7sinx-24cosx in the form ksin(x-a) where k>0 and $0\leq a\leq \frac{\pi}{2}$.

171

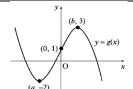
$$f(x) = 3x - 1 \text{ and } g(x) = \frac{1}{x+1}$$

Find $f(g(x))$ and $g(f(x))$.

State a suitable domain for g(f(x)).

172 The diagram shows the graph y = g(x).

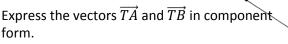
- a. Sketch y = -g(x)
- b. Sketch y = 3 g(x)



173

If
$$f = 3i + 2k$$
 and $g = 2i + 4j + 3k$, Find $|f + g|$.

174



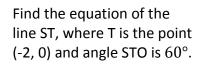
Calculate the angle between \overrightarrow{TA} and \overrightarrow{TB} .

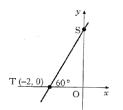
175

Prove the identity:

$$(\cos P^{\circ} + \sin P^{\circ})^{2} = 2\sin P^{\circ} \cos P^{\circ} + 1$$

176





177

Triangle ABC has vertices A(-1, 12), B(-2, -5) and C(7, -2). Find the equation of the altitude AE.

178

Show that the line with equation y = 6 - 2x in a tangent to the circle with equation $x^2 + y^2 + 6x - 4y - 7 = 0$ and find the coordinates of the point of contact of the tangent and the circle.

179

A sequence is defined by the recurrence relation
$$u_{n+1}=0.2u_n+5$$
 with $u_8=20$. Calculate u_{10} .

180

Calculate the area enclosed
between the curve
$$y = x^2 - 6x$$
 and the x-axis.

